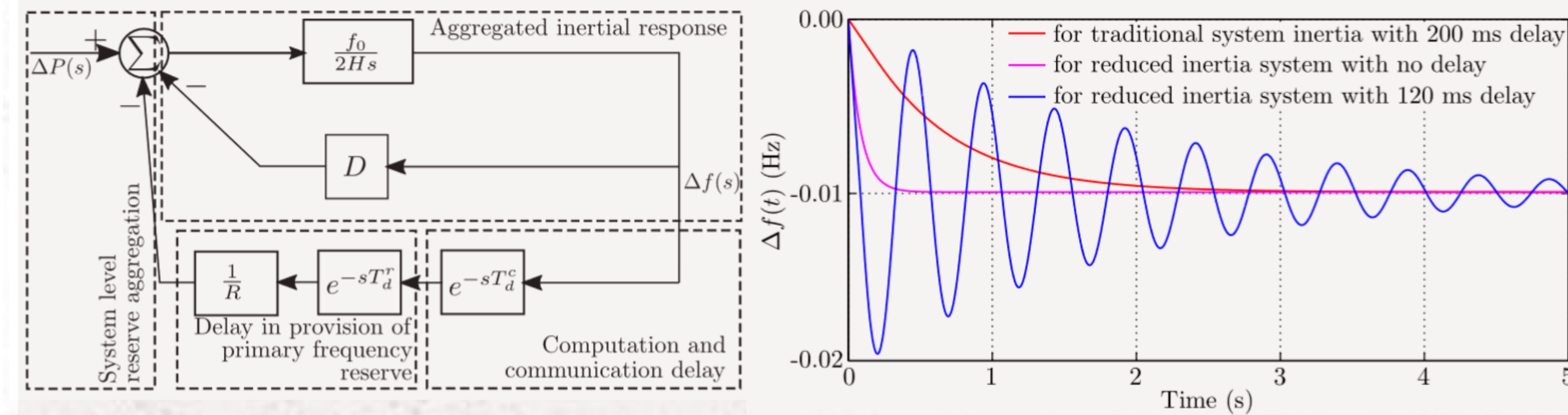
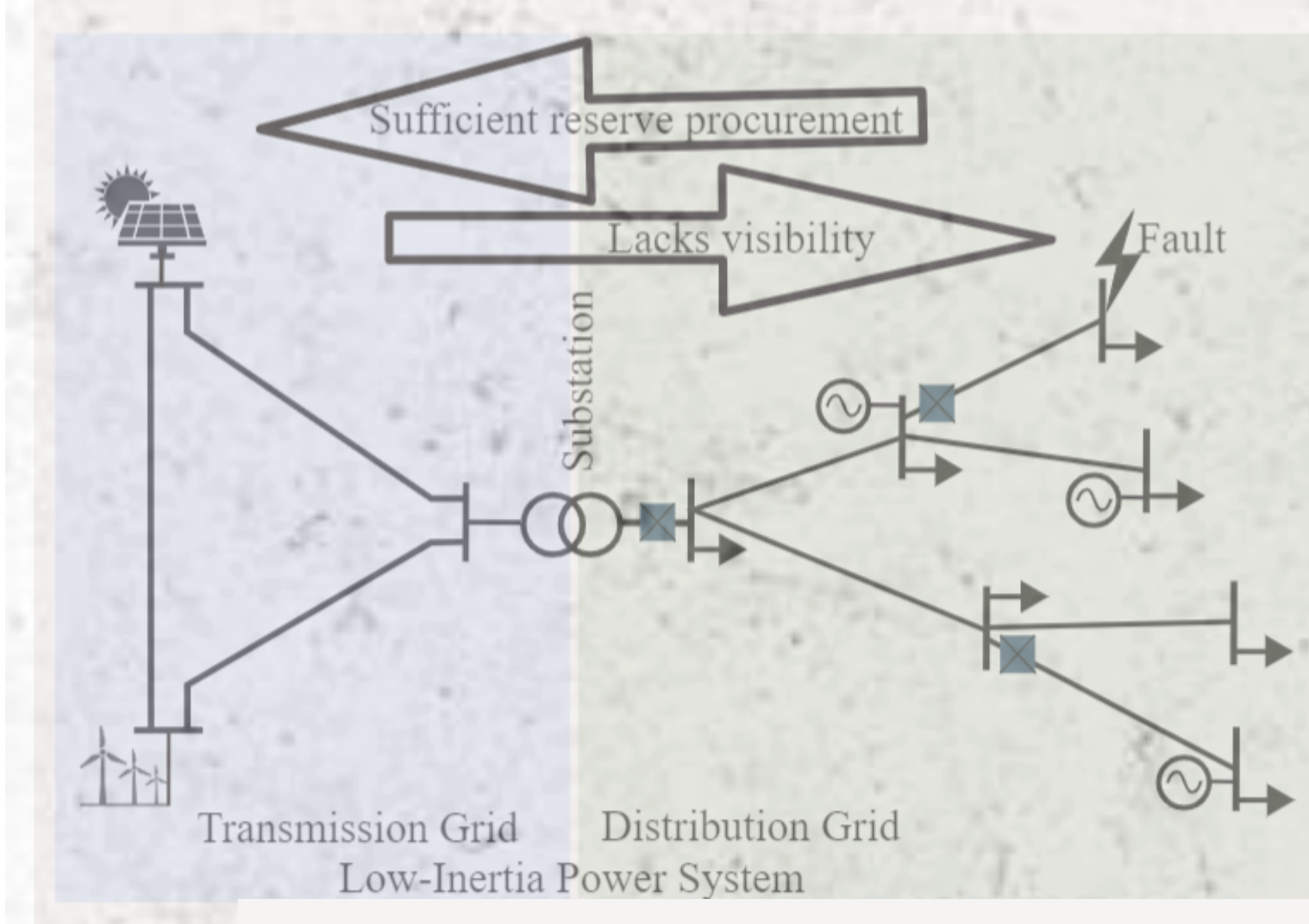


Motivation



- Increasing delay can be problematic, especially in a low-inertia system



- ISOs lack visibility inside distribution network
- How much reserve to procure?
- Who should procure?

Chance Constraint

- How much reserve is needed (load generation imbalance)?

$$P_{\xi,t}^{Imb} = \sum_{\forall q \in \mathcal{I}} (P_{q,t}^L - P_{q,t}^G) A_{\xi,q}$$

- How much reserve is available?

$$E_{\xi,t}^{Imb} = \sum_{\forall q \in \mathcal{I}} E_{q,t}^{tot} (1 - A_{\xi,q}) + E_{0,t}^{BR}$$

Local reserve Market-based reserve

- Reserve sufficiency

$$\mathbb{P} \left(\sum_{\forall \xi \in \mathcal{N}} (P_{\xi,t}^{Imb} - E_{\xi,t}^{Imb}) \mathbb{1}_{\mathcal{M}}(\xi) \leq 0 \right) \geq \kappa; \quad \forall t$$

$$\mathbb{P} \left(\sum_{\forall \xi \in \mathcal{N}} (-P_{\xi,t}^{Imb} - E_{\xi,t}^{Imb}) \mathbb{1}_{\mathcal{M}}(\xi) \leq 0 \right) \geq \kappa; \quad \forall t$$

Or, $VaR \leq 0$

Formulation

$$VaR_{\kappa} \left(\sum_{\forall \xi \in \mathcal{N}} (P_{\xi,t}^{Imb} - E_{\xi,t}^{Imb}) \mathbb{1}_{\mathcal{M}}(\xi) \right) \leq CVaR_{\kappa} \left(\sum_{\forall \xi \in \mathcal{N}} (P_{\xi,t}^{Imb} - E_{\xi,t}^{Imb}) \mathbb{1}_{\mathcal{M}}(\xi) \right) \leq 0$$

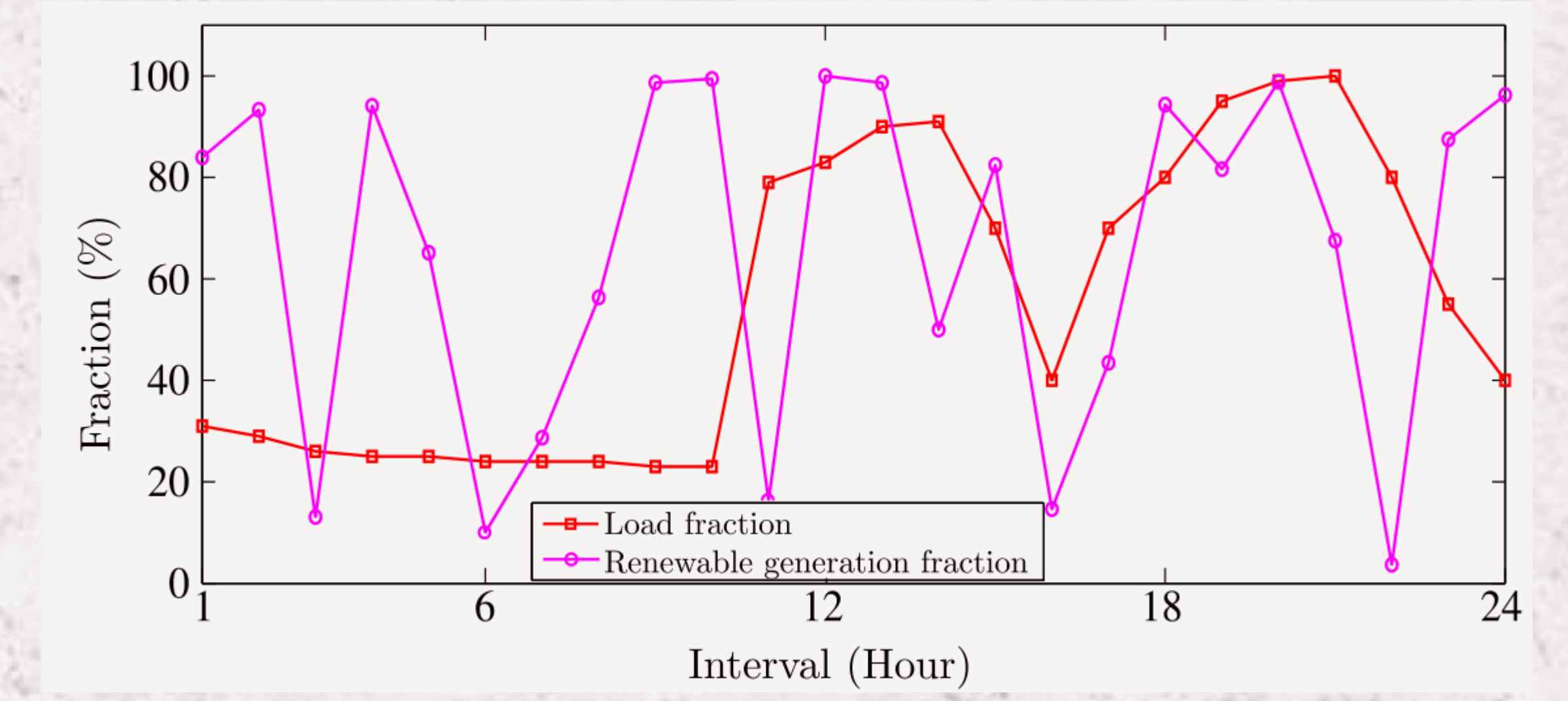
- So, we can use CVaR interchangeably with VaR

$$\Xi + \frac{1}{1 - \kappa} \sum_{\forall \xi} \mathbb{P}_{\xi} \beta_{\xi} \leq 0$$

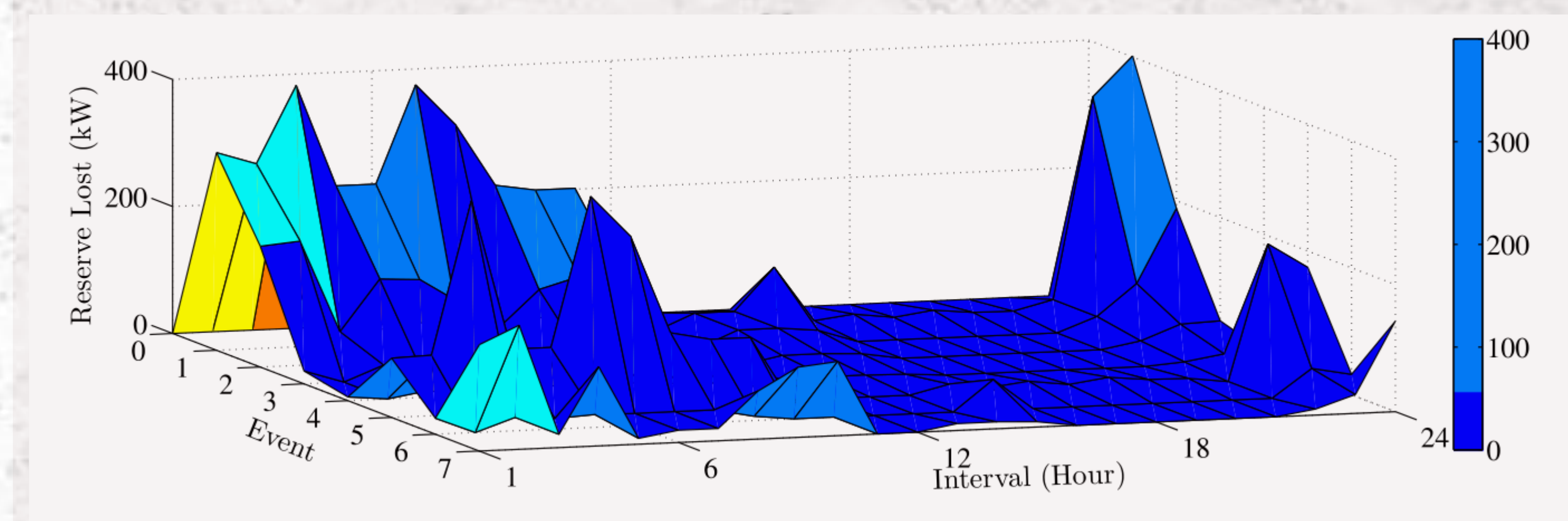
Our problem formulation is convex!

$$x_{\xi} - \Xi - \beta_{\xi} \leq 0; \beta_{\xi} \geq 0; \forall \xi$$

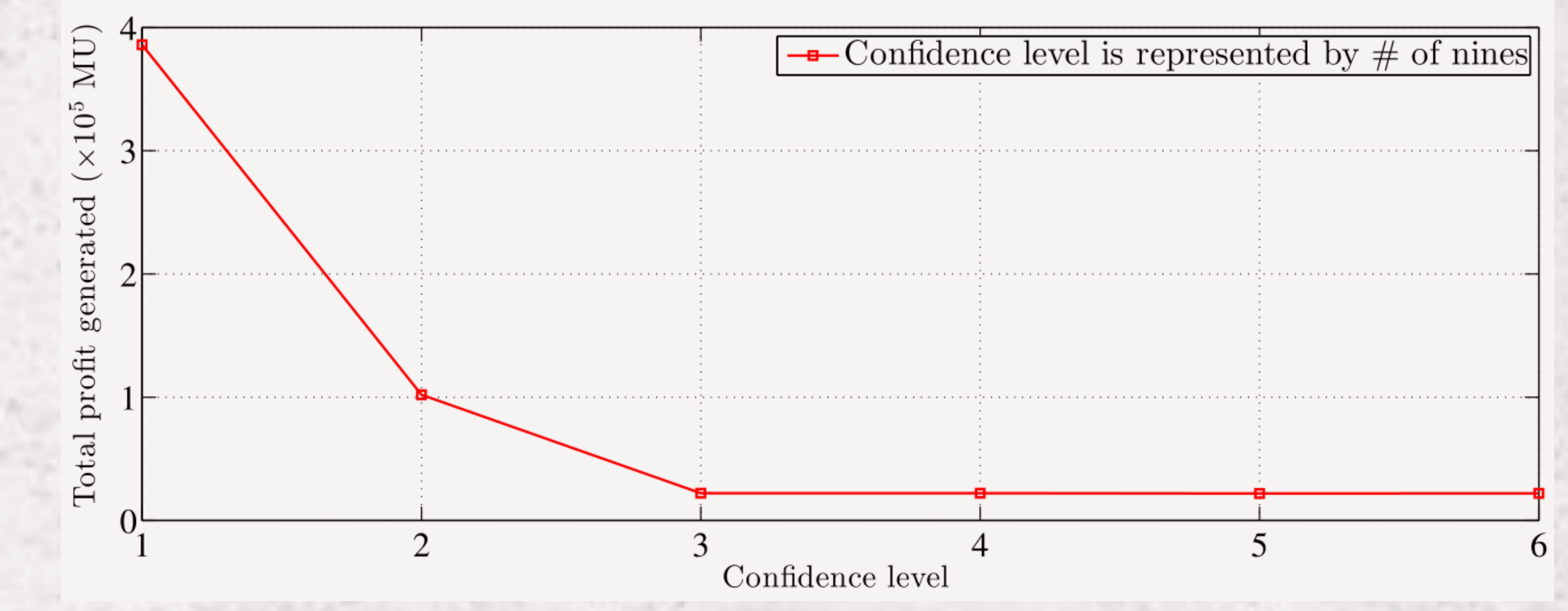
Example



Example renewable generation / load pattern

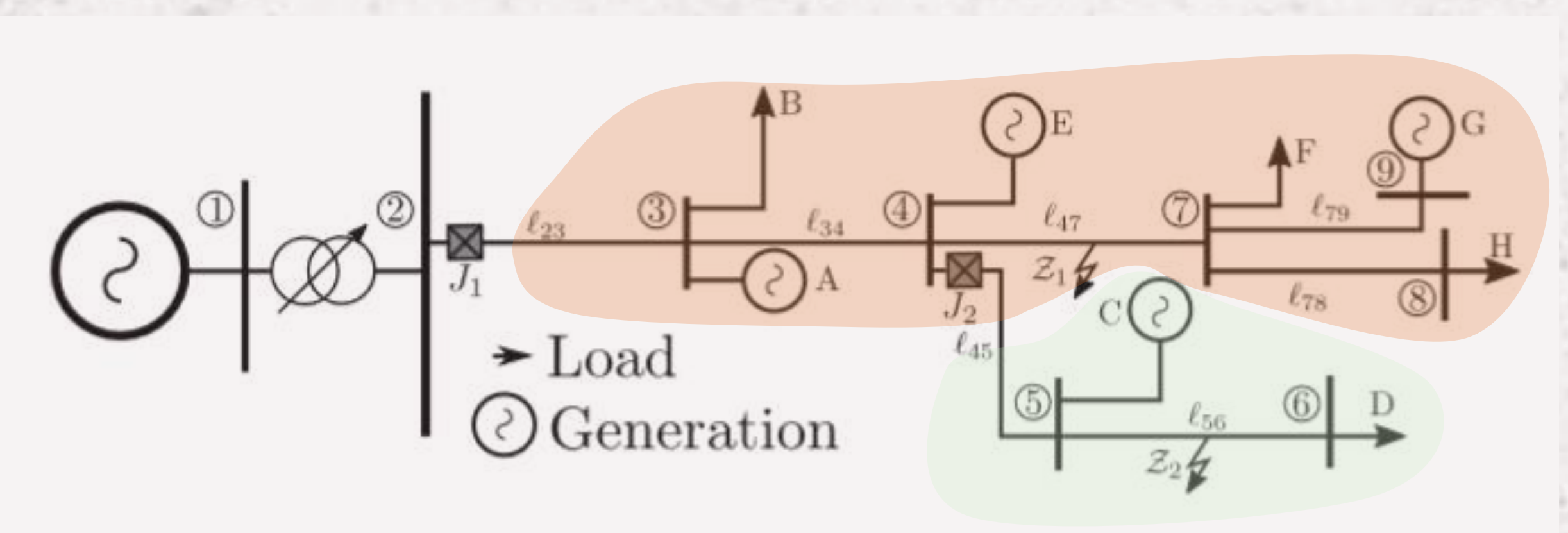


Depending upon the prices, it is worthy to procure reserve from local resources



Reserve can be procured locally under lower confidence bound

Event Identification



- Probability that none of the event occurs:

$$\mathbb{P}_{0,t} = \prod_{\forall \xi} e^{-\lambda_{\xi,t} k_t} = e^{-\sum_{\forall \xi} \lambda_{\xi,t} k_t} \approx 1 - \sum_{\forall \xi} \lambda_{\xi,t} k_t$$

- Probability that event u occurs:

$$\mathbb{P}_{u,t} = e^{-\sum_{\forall \xi, \xi \neq u} \lambda_{\xi,t} k_t} (1 - e^{-\lambda_{u,t} k_t}) \approx \left(1 - \sum_{\forall \xi, \xi \neq u} \lambda_{\xi,t} k_t \right) \lambda_{u,t} k_t \approx \lambda_{u,t} k_t$$

Discussion

- We need a risk-constrained approach to FAR provisioning due to the stochastic nature of temporary faults
- Current market structure do not account for the impact of these events
- Reserve requirements can influence the local energy schedule and raise energy costs
- The confidence level of the chance-constraint can significantly impact the overall profitability
- Effectiveness of DER integration depends significantly on policy and incentive structures; the market operators should come up with innovative structures to manage the impact of future grid events

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Link to articles:

